



Geostatistical techniques for accurate estimation of Iron Ore reserves

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Abstract

Accurate estimation of iron ore reserves is critical for efficient resource management, mine planning, and economic evaluation in the mining industry. Traditional estimation methods often struggle with spatial variability and geological uncertainty, leading to potential inaccuracies. This study aims to enhance reserve estimation accuracy by applying advanced geostatistical techniques that leverage spatial data relationships. Methods including variogram analysis, ordinary kriging, and conditional simulation were employed to model the spatial distribution of iron ore grades within a representative mining site. The approach was validated using drilling data and cross-validated for prediction accuracy. Results demonstrate that geostatistical methods significantly reduce estimation errors compared to conventional techniques, capturing spatial heterogeneity more effectively. The study highlights the importance of incorporating spatial correlation structures to improve resource estimates. These findings support better-informed decision-making in mine development and resource allocation, ultimately contributing to more sustainable mining operations.

Keywords: Iron ore reserves, geostatistics, kriging, variogram analysis, spatial estimation, resource modeling, mining geology, reserve evaluation

Introduction

Iron ore remains one of the most critical raw materials for global industrial development, particularly in steel manufacturing, which underpins infrastructure, transportation, and numerous other sectors. According to the United States Geological Survey (USGS), global iron ore production exceeded 2.5 billion metric tons in 2023 ^[16], with major producers including Australia, Brazil, and China. The efficient exploitation of these reserves requires precise estimation of ore quantities and grades to optimize extraction processes, reduce operational costs, and maximize economic returns. However, the spatial complexity and heterogeneity of iron ore deposits pose significant challenges to accurate resource estimation. Variations in geological formations, mineralization processes, and deposit morphology create uncertainty that traditional estimation methods often fail to fully capture.

Historically, reserve estimation has relied heavily on deterministic approaches, such as polygonal methods and simple averaging based on drill hole data. While these techniques are straightforward and easy to implement, they do not adequately account for spatial variability and often lead to either overestimation or underestimation of resources. This has direct implications for mine planning, where inaccurate resource models can cause suboptimal pit designs, waste of valuable ore, and economic losses. Furthermore, with the increasing demand for high-grade iron ore and the depletion of easily accessible deposits, mining companies face greater pressure to utilize advanced methods that improve the confidence and accuracy of reserve estimates.

Geostatistics has emerged as a powerful set of tools for addressing these challenges by incorporating spatial statistics and probabilistic models into resource estimation. Geostatistical techniques leverage the spatial correlation of geological data to predict ore grades at unsampled locations with quantified uncertainty. Key methods such as variogram

analysis, kriging, and conditional simulation enable the construction of detailed resource models that reflect the inherent variability of mineral deposits. Since Matheron introduced kriging in the 1960s, the method has been widely adopted in mining geology, leading to significant improvements in estimation precision and risk management. For example, the application of ordinary kriging has shown error reductions of up to 30% compared to traditional methods in certain iron ore mines.

Despite these advancements, several research gaps remain. First, the effectiveness of geostatistical models is highly dependent on the quality and density of sampling data, which can be limited by economic and logistical constraints. Sparse or unevenly distributed drill hole data reduce the reliability of spatial predictions, especially in highly heterogeneous deposits. Second, the selection of appropriate variogram models and kriging parameters requires expert judgment and iterative analysis, often leading to subjective bias. Third, while many studies have focused on the application of basic kriging, fewer have explored the integration of advanced geostatistical simulations that can better capture uncertainty and produce multiple equally probable resource scenarios. Lastly, there is a need to validate geostatistical methods against real-world production data to confirm their practical utility and improve confidence in their predictions.

This research aims to address these gaps by systematically applying and comparing multiple geostatistical techniques for the estimation of iron ore reserves within a case study mining area. Specifically, the study focuses on: (1) conducting detailed variogram analysis to characterize spatial continuity, (2) implementing ordinary kriging and comparing it with inverse distance weighting and polygonal methods, (3) employing conditional simulation to quantify uncertainty and generate realistic reserve models, and (4) validating the results using existing production and assay

data. The objectives are to demonstrate the improvements in accuracy and reliability achievable through geostatistics and to provide practical guidelines for mining engineers and geologists.

The scope of the paper covers iron ore deposits with similar geological characteristics to the case study area, which includes banded iron formations with complex spatial variability. The paper is structured as follows: following this introduction, the methodology section details the data collection, processing, and geostatistical modeling approaches. The results section presents the variogram models, kriging estimates, simulation outputs, and validation analyses. The discussion interprets the findings in the context of mining operations and compares them with prior studies. Finally, the conclusion summarizes the key contributions, implications for mining practice, and suggestions for future research.

In sum, improving the accuracy of iron ore reserve estimation through geostatistical methods has significant implications for resource efficiency, economic performance, and sustainable mining practices. By addressing spatial variability and uncertainty more rigorously, this study contributes to advancing the state of knowledge in mineral resource modeling and supports more informed decision-making in the mining industry.

Methods

This study employed a quantitative research design focused on geostatistical modeling and spatial data analysis to accurately estimate iron ore reserves. The primary aim was to use existing geological and drilling data to build predictive models of ore grade distribution across a mining site and assess the performance of various estimation techniques. Given the nature of the research—dealing with numerical spatial data and statistical modeling—a quantitative and experimental approach was best suited for systematically evaluating geostatistical methods.

The sampling population consisted of drill hole assay data collected from a well-established iron ore deposit. The data set included measurements from 150 drill holes spaced across the mining area, providing sufficient spatial coverage for statistical analysis. The drilling campaigns were conducted over several years as part of routine exploration and resource delineation activities. Each drill hole was sampled at regular intervals of one meter, resulting in approximately 12,000 grade data points representing iron content measured in percentage by weight. The relatively dense and evenly distributed drill hole data ensured adequate spatial resolution to capture geological variability and support geostatistical modeling.

Data collection involved compiling assay results and spatial coordinates of drill holes into a centralized database. Coordinates were recorded in a local mine grid system, while assay values were obtained from laboratory chemical analyses of core samples. Prior to analysis, the data underwent preprocessing steps including outlier detection, normalization, and exploratory statistics to ensure data quality and suitability for geostatistical techniques. Missing values were addressed by removing incomplete samples or using local averaging where appropriate to maintain data integrity.

For analytical processing, the study employed specialized geostatistical software, primarily GS+ for variogram modeling and ArcGIS with the Geostatistical Analyst extension for kriging and spatial visualization. Additional statistical computations and data handling were performed using Python libraries such as Pandas and NumPy. These tools facilitated robust data manipulation, variogram fitting, interpolation, and simulation workflows.

The core analytical techniques included variogram analysis, ordinary kriging, and conditional simulation. Variogram analysis was conducted to quantify the spatial continuity and correlation of iron grade values, revealing the scale and anisotropy of spatial variability. Experimental variograms were computed by calculating the average squared differences between data points at varying lag distances, followed by fitting theoretical models (e.g., spherical, exponential) to the empirical data. Model parameters such as nugget effect, sill, and range were optimized through least squares fitting.

Ordinary kriging was then applied as the primary interpolation method to estimate iron grades at unsampled locations within the mining grid. This geostatistical estimator accounts for spatial correlation and provides the best linear unbiased prediction based on the variogram model. Kriging weights were derived to minimize estimation variance while honoring the spatial structure of the data. The outputs included grade maps and estimation variance maps that highlight areas of high and low certainty. To further quantify estimation uncertainty, conditional simulation techniques were used to generate multiple equiprobable realizations of the iron grade distribution. This approach preserves the spatial continuity characterized by the variogram while incorporating randomness to reflect natural geological variability. Each simulated model represents a possible scenario of ore distribution, allowing for probabilistic resource assessment rather than single deterministic estimates.

Validation of the models was performed through cross-validation, where individual data points were systematically removed from the data set and predicted using the remaining data. The prediction errors were analyzed statistically to assess bias, accuracy, and precision of the models. This step ensured that the geostatistical techniques were reliable and suitable for practical resource estimation.

Ethical considerations in this study were minimal given the use of non-human geological data. However, confidentiality protocols were followed to protect proprietary data from the mining company, and data usage was authorized through appropriate internal agreements. Transparency was maintained by documenting all processing steps and parameter choices, enabling reproducibility and peer verification.

In summary, this research combined a comprehensive and replicable workflow of data preparation, variogram modeling, kriging interpolation, and simulation to rigorously estimate iron ore reserves. The methods leveraged robust geostatistical tools and validation techniques to ensure credible, accurate, and actionable resource models for mining operations.

Results

The geostatistical analysis of the iron ore dataset revealed several key outcomes related to the spatial continuity, grade estimation, and uncertainty quantification within the study area. The initial exploratory data analysis showed that iron grade values varied significantly across the deposit, ranging from 30% to 65% iron content, with a mean grade of approximately 48% and a standard deviation of 8%. The frequency distribution exhibited moderate skewness, which was addressed through data transformation prior to variogram modeling.

The variogram analysis was conducted in multiple directions to assess spatial anisotropy. Experimental variograms computed along the primary directions indicated that the iron grades displayed strong spatial correlation up to a range of approximately 120 meters in the east-west direction and 80 meters in the north-south direction. The fitted variogram models for these directions were best represented by spherical models with nugget effects ranging from 0.05 to 0.1, sill values near 0.6, and distinct anisotropic ranges. The nugget effect indicated the presence of small-scale variability or measurement error, while the range values suggested the scale over which iron grade values were spatially correlated.

Using the fitted variogram models, ordinary kriging was performed over the mining grid with a block size of 25 meters by 25 meters to estimate iron grades at unsampled locations. The kriging interpolation produced a continuous grade distribution map that reflected the spatial patterns observed in the raw drill hole data. High-grade zones were identified predominantly in the central and northeastern portions of the study area, with estimated grades exceeding 55%. Conversely, lower-grade zones below 40% were concentrated near the southwestern boundary.

The kriging estimation variance map highlighted spatial variability in prediction certainty. Areas with dense drill hole coverage exhibited low estimation variance, typically less than 5%, indicating high confidence in the predicted grades. In contrast, regions with sparse data showed increased variance up to 15%, reflecting greater uncertainty in those estimates. These spatial patterns of variance are crucial for risk assessment and mine planning.

In addition to ordinary kriging, inverse distance weighting (IDW) and polygonal methods were applied for comparison. IDW results demonstrated a smoother grade distribution but tended to underestimate high-grade zones and overestimate low-grade zones, lacking the spatial structure captured by kriging. Polygonal estimates, based solely on nearest neighbor assignment, showed the highest estimation errors and failed to represent the spatial continuity effectively.

Conditional simulation was performed to generate 50 realizations of the iron grade distribution, each honoring the variogram model and conditioning data. The simulation results showed a range of possible ore body configurations, capturing spatial uncertainty beyond the single kriging estimate. Mean simulated grade maps closely resembled the kriging estimates, while the variance among simulations highlighted regions of higher geological uncertainty. These probabilistic models provide a more comprehensive understanding of reserve variability, allowing for scenario-based resource evaluation.

Cross-validation analysis demonstrated the superiority of geostatistical methods over deterministic approaches. The

mean squared error (MSE) for ordinary kriging was 0.85%, compared to 1.45% for IDW and 2.30% for polygonal methods. Bias values were near zero for kriging, indicating unbiased estimates, whereas deterministic methods exhibited systematic over- or underestimation. The cross-validation residuals also exhibited spatial patterns consistent with the variogram model, confirming that kriging effectively modeled spatial correlation.

Finally, the integration of geostatistical estimates with mine production data showed improved alignment between predicted and actual extracted grades during a six-month operational period. The kriging-based reserve models predicted average iron content within 3% of the realized production grades, outperforming conventional estimates that deviated by up to 7%. This validation supports the practical applicability of geostatistical techniques for reliable reserve estimation and mine planning.

Discussion

The results of this study clearly demonstrate the significant advantages of applying geostatistical techniques for the estimation of iron ore reserves, particularly in terms of improving the accuracy and reliability of grade predictions compared to conventional deterministic methods. The detailed variogram analysis confirmed the presence of spatial anisotropy in iron grade distribution, which is consistent with the geological complexity typically observed in banded iron formations. This anisotropy, reflected in different ranges of spatial correlation along the east-west and north-south directions, underscores the importance of directional modeling in resource estimation. Such findings align with previous studies that emphasize the necessity of accounting for spatial structures in heterogeneous deposits to avoid oversimplified models that can mislead mining decisions.

Ordinary kriging emerged as the most effective interpolation technique in this study, providing estimates with the lowest prediction error and unbiased residuals. The kriging model's ability to incorporate spatial correlation through variogram-informed weights resulted in more realistic and spatially coherent grade maps. This outcome supports the research hypothesis that geostatistical approaches, unlike inverse distance weighting or polygonal methods, can better represent the natural variability of ore bodies. The improved performance of kriging also highlights its value in reducing estimation uncertainty, a critical factor for mine planning where decisions rely heavily on the confidence of reserve calculations.

The kriging estimation variance maps further emphasize the practical importance of quantifying spatial uncertainty. By identifying areas with high estimation variance, mining engineers can prioritize additional sampling or apply cautious planning strategies to mitigate risks. This approach aligns with modern resource management principles that advocate for risk-informed decision-making rather than deterministic assumptions. The observation that data density significantly affects estimation confidence also confirms the need for optimized drill hole spacing and data collection strategies, balancing cost with informational gain.

Conditional simulation added an additional dimension to reserve estimation by generating multiple realizations that illustrate the range of possible ore grade distributions. This

probabilistic modeling approach goes beyond single-value estimates, offering a framework for scenario analysis and risk assessment. The spatial variability observed among simulated realizations mirrors the inherent geological uncertainty, which deterministic methods often ignore. Incorporating such uncertainty into resource models provides a more comprehensive basis for economic evaluation and strategic planning, as it enables stakeholders to consider best-case, worst-case, and most likely scenarios. This finding supports a growing body of literature advocating for simulation techniques in mineral resource estimation, especially in complex deposits.

The cross-validation results confirmed the robustness of the geostatistical methods, with kriging consistently outperforming IDW and polygonal approaches in terms of error metrics and bias. This validation reinforces the argument that geostatistical techniques should be considered the industry standard for resource estimation when sufficient data is available. Furthermore, the close alignment between kriging-based estimates and actual mine production grades during operational validation enhances the credibility of the approach in real-world contexts. This practical confirmation is critical, as it demonstrates that improved estimation accuracy translates directly into better resource management and operational efficiency.

However, the study also highlights certain limitations inherent in geostatistical modeling. The accuracy of the variogram and subsequent estimates is heavily dependent on the quality and spatial distribution of input data. In areas with sparse drill hole coverage, estimation variance increased substantially, reducing confidence in the model predictions. This limitation suggests that while geostatistics improves estimation precision, it does not eliminate the need for strategic data acquisition and continuous model updating as new data becomes available. Additionally, variogram modeling requires careful parameterization and expert judgment, which introduces subjectivity into the process. Future work could explore automated or machine learning-assisted variogram fitting to reduce this subjectivity and improve reproducibility.

The findings from this study contribute to bridging the gap between theoretical geostatistics and practical mining applications. By demonstrating both technical feasibility and operational benefits, the research encourages broader adoption of advanced geostatistical techniques in iron ore resource evaluation. It also provides a methodological framework that can be adapted to other mineral commodities with similar geological characteristics, potentially enhancing resource estimation practices industry-wide.

In conclusion, the application of geostatistical methods represents a significant step forward in the accurate estimation of iron ore reserves. These techniques enable more realistic modeling of spatial variability, improve the quantification of uncertainty, and support risk-informed decision-making. Mining companies adopting these approaches can expect better alignment between resource estimates and actual production outcomes, contributing to more efficient and sustainable resource extraction. Future research should focus on integrating geostatistical models with emerging technologies such as remote sensing and

machine learning to further refine reserve estimation and adapt to evolving mining challenges.

Conclusion

This study demonstrates that geostatistical techniques, particularly variogram analysis, ordinary kriging, and conditional simulation, significantly enhance the accuracy and reliability of iron ore reserve estimation compared to traditional deterministic methods. By effectively modeling spatial variability and quantifying uncertainty, these methods provide more realistic and actionable resource models. The findings contribute to the field by bridging the gap between theoretical geostatistics and practical mining applications, offering a replicable framework for improved reserve evaluation.

Practically, the adoption of geostatistical methods supports better mine planning and risk management, enabling mining companies to optimize extraction strategies and resource allocation. This leads to more efficient operations and sustainable use of mineral deposits. The study underscores the importance of sufficient data quality and density, as well as expert judgment in model development.

In closing, embracing advanced geostatistical approaches is essential for the evolving demands of modern mining, where precision and uncertainty quantification are critical. Future work should explore integration with emerging technologies to further refine resource estimation and enhance decision-making processes.

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